CO and $^{13}$CO Emission Map Construction for Simulated Galaxies

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ABSTRACT

We apply photo-dissociation (PDR) molecular line emission models to the gas of simulated galaxies in post-processing mode and produce emission maps for the rotational transitions of the CO molecule and its $^{13}$CO isotope up to $J = 4 - 3$. We use these maps to investigate the occurrence and effect of mechanical feedback on the physical parameters obtained from molecular line intensity ratios. We consider two galaxy models: a small disk galaxy of solar metallicity and a lighter dwarf galaxy with 0.2 $Z_\odot$ metallicity. Elevated excitation temperature for CO(1 – 0) correlate positively with mechanical feedback, which is enhanced towards the central region of both model galaxies. The emission maps of these model galaxies are used to compute line ratios of CO and $^{13}$CO transitions. These line ratios are used as diagnostics where we attempt to match them using a single component mechanically heated equilibrium PDR. We find that PDRs ignoring mechanical feedback in the heating budget over-estimate the gas density by a factor of 100 and the far-UV flux by factors of ~ 10 – 1000. In contrast, PDRs that take mechanical feedback into account are able to fit all the line ratios for the central < 2 kpc of the fiducial disk galaxy quite well. The mean mechanical heating rate per H atom that we recover from the line ratio fits of this region varies between $10^{-27}$ – $10^{-26}$ erg cm$^{-6}$ s$^{-1}$. Moreover the mean gas density, mechanical heating rate, and the $A_V$ are recovered to less than half dex. On the other hand our single component PDR model fit is not suitable for determining the actual gas parameters of the dwarf galaxy although the quality of the fit line ratios are comparable to that of the disk galaxy.

Key words. Galaxies:ISM – (ISM:) photon-dominated region (PDR) – ISM:molecules – Physical data and processes:Turbulence

1. Introduction

Most of the molecular gas in the universe is in the form of H$_2$. However this simple molecule has no electric dipole moment. The rotational lines associated with its quadrupole moments are too weak to be observed at gas temperatures less than 100 K, where star formations occurs. This is also true for the other emission of H$_2$; hence it is hard to detect directly in cold molecular environments by applying techniques common to those used to detect warmer gas. CO is the second most abundant molecule after H$_2$, and it has been detected ubiquitously. CO forms in shielded and cold regions where H$_2$ is present. Despite its relatively low abundance, it has been widely used as a tracer of molecular gas. Solomon & de Zafra (1975) were the first to establish a relationship between CO(1 – 0) flux ($W_{\text{CO}(1-0)}$) and H$_2$ column density ($N(H_2)$). Since then, this relationship has been widely used and it is currently known as the so-called X-factor. The applicability and limitations of the X-factor are discussed in a recent review by Bolatto et al. (2013).

Environments where cool H$_2$ is present allow the existence of CO, and many other molecular species. In such regions, collisions of these molecules with H$_2$ excite their various transitions, which emit at different frequencies. The emission line intensities can be used to understand the underlying physical phenomena in these regions. These line emission can be modelled by solving for the radiative transfer in the gas. One of the most direct ways to model the emission is the application of the large velocity gradient (LVG) approximation (Sobolev 1960). LVG models model the physical state of the gas such as the density and temperature, they do not differentiate among excitation mechanisms of the gas, such as heating by shocks, UV, or X-rays, and they do not provide information about the underlying physics.

The next level of complexity involves modelling the gas as equilibrium photo-dominated regions, PDRs (Tielens & Hollenbach 1985; Hollenbach & Tielens 1999). These in turn are limited when it comes to their applicability to star forming regions and star-bursts. Modelling of Herschel and other observations for e.g. NGC 253, NGC 6240 and M82, using these PDRs show that these models lack particular heating sources, such as heating due to AGN or enhanced cosmic ray ionization (Maloney et al. 1996; Komossa et al. 2003; Martin et al. 2006; Papadopoulos 2010; Meijerink et al. 2013; Rosenberg et al. 2014; among many others). Another heating source which is not accounted for in PDR modelling and is relevant to this paper is mechanical heating due to turbulence (Loenen et al. 2008; Aalto 2013).

Various attempts have been made in this direction in modelling star-forming galaxies and understanding the properties of the molecular gas. But because of the complexity and resolution requirements of including the full chemistry in the models, self-consistent galaxy-scale simulations have been limited mainly to CO (Kravtsov et al. 2002; Wada & Tomisaka 2005; Narayanan et al. 2008; Pelupessy & Papadopoulos 2009; Xu et al. 2010; Pérez-Beauvais et al. 2011; Narayanan et al. 2011; Shetty et al. 2011; Feldmann et al. 2012; Narayanan & Hopkins 2013).

The rotational transitions of CO up to $J = 4 - 3$, predominantly probe the properties of gas with densities in the range of $10^2$ – $10^3$ cm$^{-3}$, and with temperatures around ~ 50K; higher $J$ transitions probe denser and warmer molecular gas around ~ 200K for the $J = 10 - 9$ transition. In addition to
high-\(J\) CO transitions other high-density tracers, such as CS, CN, HCN, HNC and HCO\(^+\), are good probes of cold gas with \(n \sim 10^6\) cm\(^{-3}\). Thus having a broad picture on how these species and their line emission are related to their environment provide a full picture on the underlying physical processes.

In Kazandjian et al. (2012, 2013) we studied the effect of mechanical feedback on diagnostic line ratios of CO, \(^{13}\)CO and other high density tracers for grids of mechanically heated PDR models in a wide parameter space relevant to quiescent disks as well as turbulent galaxy centres. We found that molecular line ratios between \(J \geq 4 - 3\) and lower transitions are good diagnostics of mechanical heating. In this paper we build on our findings in Kazandjian et al. (2013) to apply them to the chemistry models to simulated galaxies with sub-grid modelling in post processing mode to construct CO and \(^{13}\)CO maps for transitions up to \(J = 4 - 3\). Our approach is similar to that by Pérez-Beaujouits et al. (2011) where the sub-grid modelling is done using PDR modelling that includes a full chemical network based on (Le Teuff et al. 2000), which is not the case for the other references mentioned above. The main difference of our work from Pérez-Beaujouits et al. (2011) is that our sub-grid PDR modelling takes into account the mechanical feedback in the heating budget; on the other hand we do not consider any X-ray heating effects due to any AGN. The synthetic maps are processed in a fashion that simulates what observers would measure. These maps are used as a guide to determine how well diagnostics such as the line ratios of CO and \(^{13}\)CO can be used to constrain the presence and magnitude of mechanical heating in actual galaxies.

In the method section we start by describing the galaxy models used, although our method is generally applicable to other grid and SPH based simulations. We then proceed by explaining the procedure through which the synthetic molecular line emission maps were constructed. In the results section we study the relationship and the correlation between the luminosities of CO, \(^{13}\)CO, and H\(_2\). We also present maps of the line ratios of these two molecules and see how mechanical feedback affects them, how well the physical parameters of the molecular gas can be determined when the gas is modelled as a single PDR with and without mechanical feedback. In Particular we try to constrain the local average mechanical heating rate, column density and radiation field and compare that to the input model. We finalize with a discussion and conclusions.

2. Methods

In order to construct synthetic emission maps of galaxies, we need two ingredients (1) A model galaxy which provides us with the state of the gas (2) a prescription to compute the various emission of the species. We start by describing the galaxy models in Section 2.1 along with the assumptions used in modelling the gas. The parameters of the gas which are necessary to compute the emission of the species and the properties of the model galaxies chosen are described in Section 2.2. In Section 2.3 we describe the method with which the sub-grid PDR modelling was achieved, from which the emission of the species were computed. Sub-grid modelling is necessary since simulations which would resolve scales where H/H\(_2\) transitions occur (Tielens & Hollenbach 1985), and where CO forms, need to have a resolution less than \(\sim 0.01\) pc. This is not the case for our model galaxies, but is achieved in our PDR models. The procedure for constructing the emission maps is described in Section 2.4.

2.1. Galaxy models

In this paper, we will use the model galaxies of Pelupessy & Papadopoulos (2009) which are TreeSPH simulations of isolated dwarf galaxies in a steady state. The simulation code calculates self-gravity using an Oct-tree code (Barnes & Hut 1986) and gas dynamics using the softened particle hydrodynamics (SPH) formalism (see e.g. Monaghan 1992), in the conservative formulation of Springel & Hernquist (2002). It uses an advanced model for the ISM, a star formation recipe based on a Jeans mass criterion, and a well-defined feedback prescription. More details of the code and the simulations can be found in Pelupessy & Papadopoulos (2009). Below we will summarise main ingredients.

The ISM model used in the dynamic simulation code is similar, albeit simplified, to that of Wolfire et al. (1995, 2003). It solves for the thermal evolution of the gas including a range of collisional cooling processes, cosmic ray heating and ionization. It tracks the development of the warm neutral medium (WNM) and the cold neutral medium (CNM) HI phases. The latter is where densities, \(n > 10^3\) cm\(^{-3}\), and low temperatures, \(T < 100\) K, allow the H\(_2\) molecules to form. Our assumption is that the short time-scales in these dense regions, which are associated with non-equilibrium effects, may play an important role in the formation and emission of the molecular species. For instance, in star-bursts in galaxy centres, the chemical time-scale of H\(_2\) formation out of HI (Hollenbach & Tielens 1999) is comparable to the time-scale of the build-up of the UV field (Parravano et al. 2003), the orbital period of molecular gas in the central few parsec of galaxy centres (Kim et al. 2006), the dynamical time-scale of spherical clouds, as well as the time-scale of the occurrence of these star-bursts.

The FUV luminosities of the stellar particles, which are needed to calculate the photoelectric heating from the local FUV field, are derived from synthesis models for a Salpeter IMF with cut-offs at 0.1 Msun and 100 Msun by Bruzual A. & Charlot (1993), and updated by Bruzual & Charlot (2003) population. Dust extinction of UV light is not accounted for, other than that from the natal cloud. For a young stellar cluster we decrease the amount of UV extinction from 75\% to 0\% in 4 Myr (see Parravano et al. 2003).

For an estimate of the mechanical heating rate we extract the local dissipative terms of the SPH equations, the artificial viscosity terms (Springel 2005). These terms describe the thermalization of shocks and random motions in the gas, and are in our model ultimately derived from the supernova and the wind energy injected by the stellar particles that are formed in the simulation (Pelupessy 2005). We realize that this method of computing the local mechanical heating rate is very approximate. To be specific: this only crudely models the actual transport of turbulent energy from large scales to small scales happening in real galaxies, but for our purposes it suffices to obtain an order of magnitude estimate of the available energy and its relation with the local star formation.

We selected two galaxy types from the sweep of galaxy models by Pelupessy & Papadopoulos (2009), and applied our PDR models to them. These galaxies are star-forming galaxies and have metallicities representing typical dwarfs and disk-like galaxies, which enable us to study typical star-bursting regions. The first model galaxy is a dwarf galaxy with low metallicity \((Z = 0.2 Z_\odot)\). The second model is a heavier, disk like, galaxy with metallicity \((Z = Z_\odot)\). The basic properties of the two simulations are summarized in Table I.
2.2. Ingredients for further sub-grid modelling

While our method of constructing molecular emission maps is generally applicable to grid based or SPH hydrodynamic simulations of galaxies, we use the simulations of Pelupessy & Papadopoulos (2009) since they provide all the necessary ingredients to allow for our sub-grid modelling prescription. It consists of post-processing the snapshots of the hydrodynamic density field, to produce realistic molecular line emission maps. Our method is applicable to a simulation if it provides a number of physical quantities for each of the resolution elements (particles, grid cells): the densities resolved in the simulation must reach \( n \sim 100 - 1000 \text{ cm}^{-3} \) in order to produce reliable CO and \(^{13}\text{CO} \) emission maps up to \( J = 4 - 3 \), and the simulation must provide estimates of the environmental temperature, far-UV field flux and local mechanical heating rate. In essence, the simulation must provide realistic estimates of the CNM environment in which the molecular clouds develop. In the next section we describe in detail the assumptions with which the CNM was modelled. A number of such galaxy models exist (see the Introduction for references), and with the increase in computing power, more such simulations, also simulating the cosmological context, are expected to become available. Pelupessy & Papadopoulos (2009) present a sweep of SPH models of disk and dwarf galaxies. We note that the gas temperature estimated from the PDR models is not the same as the gas temperature of the SPH particle from the simulation. The reason for this is the assumption that the PDR is present in the sub-structures of the SPH particle. This sub-structure is not resolved by the large scale galaxy simulations, hence not probed. We have compared the temperature at the surface of the PDR to that of the SPH particle, where we find a good agreement between them. This is a good check since the SPH particle provides a boundary condition to the embedded PDR model. We want to stress that we can apply our methodology to any simulation that fulfils the above criteria.

2.3. Sub-grid PDR modelling in a post-processing mode

In order to model the emission emanating from the SPH particles, we model the substructure that is present on scales below that probed by the SPH particles using a sub-grid model. For this we assume (1) local dynamical and chemical equilibrium and (2) that the substructure where \( \text{H}_2 \) forms complies to the scaling relation of Larson (1981), from which the prescription, by Pelupessy et al. (2006), of the mean \( A_V \) given in Eq. (1) is derived.

\[
< A_V > = 3.344 Z \left( \frac{P_c/k_B}{10^{8} \text{ cm}^{-3} K} \right)^{1/2} 
\]

\( Z \) is the metallicity of the galaxy in terms of \( Z_\odot \), \( P_c \) is the boundary pressure of the SPH particle and \( k_B \) is the Boltzmann constant. Using the boundary conditions as probed by the SPH particles and this expression for the mean could \( A_V \), we proceed to solve the for the chemical and thermal equilibrium using PDR models.

We assume a 1D semi-infinite plane-parallel geometry for the PDR models whose equilibrium is solved for using the Leiden PDR-XDR code of Meijerink & Spaans (2005). Each semi-infinite slab is effectively a finite slab illuminated from one side by a FUV source. This is of course an approximation, where the contribution of the FUV sources from the other end of the slab is ignored, and the exact geometry of the cloud is not taken into account. The chemical abundances of the species and the thermal balance along the slab are computed self-consistently at equilibrium, where the UMIST chemical network (Le Teuff et al. 2000) is used. In this paper we keep the elemental abundance ratio of \(^{12}\text{C}/^{13}\text{C} \) fixed to a value of 40, that is the lower limit of the suspected range in the Milky way. This ratio is important in the optically thin limit of the CO line emission at the edges of the galaxies. It plays a less significant role in the denser central regions of galaxies. We have outlined the major assumptions of the PDR models used in this paper, for more details on these see Meijerink & Spaans (2005); Kazandjian et al. (2012, 2013).

The main parameters which determine the intensity of the emission of a PDR are the gas number density \( n \), the FUV flux \( (G) \) and the depth of the cloud measured in \( A_V \). In our PDR models we also account for the mechanical feedback, we refer these as mechanically heated PDRs (mPDR), which affects the chemical abundances of species (Loenen et al. 2008; Kazandjian et al. 2012), as well as their emission (Kazandjian et al. 2013). Hence the fourth important parameter required for our PDR modelling is the mechanical feedback \( (\Gamma_{\text{mech}}) \). In addition to these four parameters, metallicity plays an important role, but this is taken constant throughout each model galaxy (See Table 1). The SPH simulations provide local values for \( n, G \), and \( \Gamma_{\text{mech}} \).

Based on the PDR model grids in Kazandjian et al. (2013) we can compute the line emission intensity of CO and \(^{13}\text{CO} \) given the four parameters \( (n, G, \Gamma_{\text{mech}}, A_V) \) at a given metallicity. We briefly summarize the method by which the emission was computed by Kazandjian et al. (2013). For each PDR model the column densities of CO and \(^{13}\text{CO} \) have been mapped in the model grids. Assuming the LVG approximation, these quantities are used as input to RADIEx (Schoier et al. 2005) which computes the line intensities. In the LVG computations a micro-turbulence line-width of 1 km s\(^{-1} \) was used. Comparing this line width to the velocity dispersion of the SPH particles, we see that the velocity dispersion for particles with \( n > 10 \text{ cm}^{-3} \), where most of the emission comes from and which have \( A_V > 5 \text{ mag} \), is on the order of unity. The choice of the micro-turbulence line width has a minor effect on diagnostic line ratios.

In this paper, the parameter space used by Kazandjian et al. (2013) was extended to include \( 10^{-3} \le n < 10^6 \text{ cm}^{-3} \), \( 10^{-3} < G < 10^6 \), where \( G \) is measured in units of \( G_0 = 1.6 \times 10^{-3} \text{ erg cm}^{-2} \text{ s}^{-1} \). Moreover the emission was tabulated for \( A_V = 0.01, 0.1, 1...30 \text{ mag} \). The range in \( \Gamma_{\text{mech}} \) was wide enough to cover all the states of the SPH particles. For each emission line of CO and \(^{13}\text{CO} \) we constructed 4D interpolation tables. Consequently given any set of the four PDR parameters, for each SPH particle, we can compute the intensity of all the lines of these species. About 0.1% of the SPH particles had their parameters outside the lower bounds of the interpolation tables, mainly \( n < 10^3 \text{ cm}^{-3} \) and \( G < 10^{-3} \). The disk galaxy consists of \( 2 \times 10^6 \) particles half of which contribute to the emission; the surface temperature of the other half is larger than \( 10^4 \text{K} \) which is caused by high \( \Gamma_{\text{mech}} \) where no transition from H to H\(_2\) occurs in the PDR, thus CO and \(^{13}\text{CO} \) are under-abundant. We ignore these SPH particles since they do not contribute to the mean flux of the emission maps and the total luminosities.

<table>
<thead>
<tr>
<th>abrv</th>
<th>name</th>
<th>mass (M(_\odot))</th>
<th>Z (Z(_\odot))</th>
<th>gas fraction</th>
</tr>
</thead>
<tbody>
<tr>
<td>dwarf</td>
<td>coset2</td>
<td>10(^{10})</td>
<td>0.2</td>
<td>0.01</td>
</tr>
<tr>
<td>disk</td>
<td>coset9</td>
<td>10(^{10})</td>
<td>1.0</td>
<td>0.1</td>
</tr>
</tbody>
</table>

Table 1: Properties of the galaxies used.
The use of interpolation tables in computing the emission is compelled by CPU time limitations. Computing the equilibrium state for a PDR model consumes, on average, 30 seconds. Most of the time, about 50%, is spent in computing the equilibrium state up to $A_V = 1$ mag near the H/H$_2$ transition zone. Beyond $A_V = 1$ mag, the solution advances much faster. Finding the equilibria for a large number of SPH particles requires a prohibitively long time, thus we resort to interpolating. Although interpolation is less accurate, it does the required job. On average it takes 20 seconds to process all these SPH particles and produce an emission map, for each of the line emission of CO and $^{13}$CO, with the scripts running serially on a single core.

2.4. Construction of synthetic emission maps and data cubes

The Construction of the flux maps is achieved by the following steps:

1. Bin the region of interest over a spatial domain.
2. For each bin (pixel) compute the mean flux in units of energy per unit time per unit area.
3. Repeat steps 1 and 2 for each emission line.

In practice a flux map is constructed from the brightness temperature of a line, measured in K, that is spectrally resolved over a certain velocity range. This provides a spectrum at a certain pixel as a function of velocity. The integrated spectrum over the velocity results in the flux. The velocity coordinate, in addition to the spatial dimensions projected on the sky, at every pixel can be thought of as a third dimension; hence the term “cube”. Using a flux map, for a certain line computed from the simulation, we can do the opposite and construct the data cube. Each SPH particle has a different line-of-sight velocity and a common FWHM micro-turbulence line width of 1 km s$^{-1}$. By adding the contribution of the Gaussian spectra of all the SPH particles within a pixel, we can construct a spectrum for that pixel. This procedure can be applied to all the pixels of our synthetic map producing a synthetic data cube. The main assumption in this procedure is that the SPH particles are distributed sparsely throughout each pixel and in line of sight velocity space. We can estimate the number density of SPH particles per pixel per line-of-sight velocity bin by considering a typical pixel size of ~ 1 kpc and a velocity bin equivalent to the adopted velocity dispersion. The typical range in line of sight velocities is from -50 to +50 km/s, which results in 100 velocity bins. With an average number of 5000 SPH particles in a pixel, the number density of SPH particles per pixel per velocity bin is 50. The scale size of an SPH particle is on the order of ~ 1 pc, which is consistent with the size derived from the scaling relation of Eq-1 by (Larson 1981) by using a velocity dispersion of 1 km/s. Thus the ratio of the projected aggregated area of the SPH particles to the area of the pixel is $\sim 10^{-4}$. This can roughly be thought of as the probability of two SPH particles overlapping along the line of sight within 1 km/s.

3. Results

3.1. Emission maps

In Figure[1] we show the emission maps, of the first rotational transition of CO and $^{13}$CO, for the model disk and dwarf galaxy. These maps were constructed using the procedure described in Section 2.3. Emission in these maps trace the molecular gas. As the density and temperature of the gas increases towards the inner regions, the emission is enhanced. By comparing the corresponding top and bottom panels of Figure[1] we see that the emission of the dwarf galaxy is significantly weaker than that of the disk galaxy. The gas of the dwarf galaxy is 10 times lighter than the disk galaxy’s; moreover, the metallicity of the dwarf galaxy is 5 times lower than that of the disk galaxy. Hence the column densities of CO and $^{13}$CO are about 100 times lower in the former galaxy. In the PDR sub-grid modelling of the dwarf galaxy the mean gas temperatures used to compute the emission is ~ 10 times lower compared to the disk galaxy, which results in weak excitation of the upper levels of the molecules through collisions. All these factors combined result in reduced molecular luminosity in the dwarf galaxy, which is $\sim 10^4$ times weaker than that of the disk galaxy.

We demonstrate the construction the data cube, described in Section 2.4, by presenting the CO(1–0) emission map of the disk galaxy in Figure[2]. These maps provide insight on the motion of the individual clouds along the line-of-sight. In the coordinate system we chose, negative velocities correspond to gas moving away from the observer, where the galaxy is viewed face-on in the sky. Thus the velocities of the clouds are expected to be distributed around a zero mean. The width in the velocity distribution varies depending on the spatial location in the galaxy. For example, at the edge of the galaxy the gas is expected to be quiescent, with a narrow distribution in the line-of-sight velocities ($V_{los}$). This is seen clearly in the channel maps $|V_{los}| = 20$ km s$^{-1}$, where the CO(1–0) emission is too weak outside the $R > 3$ kpc region. In contrast the emission of these regions are relatively bright in the $|V_{los}| = 0$ km s$^{-1}$ map. In the inner regions, $R < 1$ kpc, the CO(1–0) emission is present even in the 40 km s$^{-1}$ channel, which is a sign of the wide dynamic range in the velocities of the gas at the central parts of the galaxy.

The relationship between mechanical feedback, excitation temperature, $T_{ex}$ (see Eq-10 in van der Tak et al. (2007)) of the CO(1–0) line and the distance of the molecular gas from the centre of the galaxy ($R$) is illustrated in Figure[3]. We plot the averages of $\Gamma_{mech}/n$, the mechanical heating rate per H nucleus, and the mean $T_{ex}$ of the SPH particles in each pixel of the emission maps. $T_{ex}$ for each SPH particle is a by-product of the RADEX LVG computations (Schöier et al. 2005). We highlight the two obvious trends in the plots: (a) The mechanical heating per H nucleus increases as the gas is closer to the centre, (b) The excitation temperature correlates positively with mechanical feedback and correlates negatively with distance from the centre of the galaxy. It is also interesting to note that, on average, the SPH particles with the highest $\Gamma_{mech}/n$ have the highest excitation temperatures and are the closest to the centre, see red points in the middle panel of Figure[3]. On the other hand, gas situated at $R > 3$ kpc has average excitation temperatures less than 10 K and approaches 2.73 K, the cosmic microwave background temperature we chose for the LVG modelling, at the outer edge of the galaxy. This decrease in the excitation temperature is not very surprising, since at the outer region CO is not collisionally excited due to collisions with H$_2$ which has a mean abundance 10 times lower than that of the central region. Collisional excitation depends strongly on the kinetic temperature of the gas. In Kazandjian et al. (2012) it was shown that small amounts of $\Gamma_{mech}$ are required to double the kinetic temperature of the gas in the molecular zone, where most of the molecular emission originate. But $\Gamma_{mech}$ is at least 100 times weaker in the outer region compared to the central region, which renders mechanical feedback ineffective in collisionally exciting CO.
**3.2. The X factor: Correlation between CO emission and H$_2$ column density**

Since H$_2$ cannot be observed through its various transitions in cold molecular gas whose $T_{\text{kin}} < 100$ K, astronomers have been using its proxy molecule CO to derive the molecular mass in the ISM of galaxies. It has been argued that the relationship between CO(1-0) flux and $N$(H$_2$) is more or less linear (Solomon et al. 1987; Bolatto et al. 2013, and references therein) with $X_{\text{CO}} = N$(H$_2$)/$W_{\text{CO}(1-0)}$ nearly constant, where the proportionality factor $X_{\text{CO}}$ is usually referred to as the $X$-factor. The typical $X_{\text{CO}}$ to the Milky Way, $X_{\text{CO,MW}}$, is $\sim 2 \times 10^{20}$ cm$^{-2}$ (K km s$^{-1}$)$^{-1}$ (Solomon et al. 1987). By using the emission map of CO(1-0) presented in Figure [1] and by estimating the mean $N$(H$_2$) throughout the map from the PDR models, we test this relationship in Figure [4].

It is clear that only for pixels with $W_{\text{CO}(1-0)} > 10$ K km s$^{-1}$ $X_{\text{CO}}$ approaches $X_{\text{CO,MW}}$. These pixels are located within $R \lesssim 2$ kpc of the disk galaxy, and $R \lesssim 0.2$ kpc of the dwarf galaxy. Whenever $W_{\text{CO}(1-0)} < 10$ K km s$^{-1}$, $X_{\text{CO}}$ increases rapidly reaching $\sim 1000X_{\text{CO,MW}}$. Looking closely at pixels within $W_{\text{CO}(1-0)}$ intervals of [0,1], [1,10] and $>10$ K km s$^{-1}$ we see that the gas average densities in these pixels are $\sim 20, 80$ and $300$ cm$^{-3}$ respectively. This indicates that as the gas density becomes closer to the critical density of the CO(1-0) transition, which is $\sim 2 \times 10^{3}$ cm$^{-3}$, $X_{\text{CO}}$ converges to that of the Milky Way. This is not surprising since as the density of gas in-
Fig. 3: (Left) Mean mechanical heating per hydrogen nucleus as a function of distance from the centre of the disk galaxy. (Centre) Mean excitation temperature of the CO(1-0) line as a function of mechanical heating rate per hydrogen nucleus. (Right) Mean excitation temperature of the CO(1-0) line as a function of the distance from the centre of the disk galaxy. The different colours correspond different galactocentric distance intervals. Red, green blue and cyan correspond to intervals [0, 1], [1, 2] [2,3] and [3, 8] kpc respectively.

Fig. 4: N(H₂) vs. CO(1-0) flux of the synthetic emission maps. The blue and red points correspond to the pixels of the disk and dwarf galaxies, respectively. The solid black line is the W_CO(1-0) = X_CO,MW X(H₂) curve, with the observed ±30% uncertainty band shown by the black dashed lines. X_CO for pixels with W_CO(1-0) < 10 K km s⁻¹ diverges from that of the Milky way, where the mean X_CO for the pixels is plotted in green. We note that 99% of the luminosity of the disk galaxy emanates from pixels whose W_CO(1-0) > 1 K km s⁻¹ indicated by the dot-dashed line.

With a smaller abundance of CO in comparison to the disk galaxy, thus a lower W_CO(1-0). This results in an X_CO which is 10 to 100 times higher than that of the Milky Way (Leroy et al. 2011). Our purpose of showing Figure 4 is to check the validity of our modelling of the emission. Maloney & Black (1988) provide a more rigorous explanation on the W_CO(1-0) and N(H₂) relationship.

3.3. Higher J-transitions

So far we have only mentioned the CO(1-0) transition. The critical density of this transition is 2 x 10³ cm⁻³. The maximum density of the gas in our simulations is ~ 10⁴ cm⁻³. It is necessary to consider higher J transitions in probing this denser gas. The critical density of the CO(4-3) transition is ~ 10⁵ cm⁻³, which corresponds to densities 10 times higher than the maximum of our model galaxies. Despite this difference in densities the emission of this transition and the intermediate ones, J = 2−1 and J = 3−2, are bright enough to be observed due to collisional excitation mainly with H₂. To have bright emission from these higher J transitions, it also necessary for the gas to be warm enough, with T_Kin > 50 K, so that these levels are collisionally populated. In Figure 5 we show the luminosities of the line emission, up to J = 4−3, of CO and ¹³CO emanating from the disk and dwarf galaxies. In addition to that, we present the luminosity of the inner, R < 0.5 kpc, region of the disk galaxy where Γ_mech is enhanced compared to the outer parts. This allows us to understand the trend in the line ratios and how they spatially vary and how mechanical feedback affects them, see next section. The ladders of both species are somewhat less steep for the central region, which can be seen in comparing the black and red curves of the disk galaxy in Figure 5. Hence the line ratios for the high-J transitions to the low-J transitions are larger in the central region. This effect of Γ_mech was also discussed by Kazandjian et al. (2013, submitted), who also showed that line ratios of high-J to low-J transitions are enhanced in regions where mechanical heating is high: which is also the case for the central parts of our disk galaxy. We will look at line ratios and how they vary spatially in Section 3.4.

3.4. Diagnostics

In this section we use synthetic emission maps, for the J > 1−0 transitions, constructed in a similar fashion as described in Section 3.3. These maps are used to compute line ratios among CO and ¹³CO lines where we try to understand the possible
ranges in diagnostic quantities. This can help us recover physical properties of a partially resolved galaxy.

In Figure 5, we show ratio maps for the various transitions of CO and 13CO. In these maps, line ratios generally exhibit uniform distributions in the regions where $R < 2$ kpc. This uniform region shrinks down to 1 kpc as the transition in denominator becomes higher. This is clearly visible when looking at the corresponding 13CO/CO transitions in the panels along the diagonal of Figure 6. This is also true for the CO/CO transitions in the first and the rows. Exciting the $J > 1$ transitions requires enhanced temperatures, where $T_{\text{mech}}$ plays an important role, in addition to H$_2$ densities higher than $10^3$ cm$^{-3}$. Such conditions are typical to the central 2 kpc region but not for the outer regions. Hence diminishing emission of $J > 1$ results in the compact peaks that we mentioned. The peak value of the line ratios of CO/CO transitions at the centre is around unity, compared to 0.1–0.3 for ratios involving transitions of 13CO/CO. Since $J > 1$ transitions are weakly excited outside the central region, the line ratios decrease for e.g. by factors of 3 to 10 towards the outer edge of the galaxy for CO(2-1)/CO(1-0) and CO(4-3)/CO(1-0) respectively. Another consequence of the weak collisional excitation of CO and 13CO is noticed by looking again at the 13CO/CO transitions along the diagonal panels of Figure 6, where the small scale structure of cloud clumping, outside the central region becomes evident by comparing the 13CO (1-0)/CO(1-0) to 13CO (4-3)/CO(4-3). This dense gas is compact and occupies a much smaller volume and mass, approximately 10% by mass.

Similar line ratio maps can be constructed to the dwarf galaxy which are presented in Figure A in the Appendix. These maps can be used to constrain the important physical parameters of the gas of both model galaxies, as we will demonstrate in the next section.

4. Application: Modelling extragalactic sources using PDRs and mechanical feedback

Now that we have established the spatial variation of diagnostic line ratios in the synthetic maps, we may use them to recover the physical parameters of the molecular gas that is emitting in CO and 13CO.

The synthetic maps that we have constructed assume a high spatial resolution of 100 $\times$ 100 pixels, where the size of our model disk galaxy is $\sim$ 16 kpc. If we assume that the galaxy is in the local universe at a fiducial distance of 3 Mpc, the same distance chosen by (Pérez-Beaupuits et al. 2011), which is also the same distance of the well known galaxy NGC 253, then it is necessary to have an angular resolution of 1" to obtain such a resolution. This can be easily achieved with ALMA whose highest angular resolution is 0.01" in its widest configuration. In order not to restrict ourselves to galaxies in the local universe we adopted a resolution of 21 $\times$ 21 which corresponds to a pixel size of $\sim$ 0.8 kpc. This resolution places our galaxy five times further at the same angular resolution of 1".

In the top panel in Figure 7, we show the normalized $W_{\text{CO}(1-0)}$, normalized with respect to the peak flux, with an overlaid mesh of the resolution mentioned before. Each pixel in the mesh contains, on average, a few thousand SPH particles. For simplicity, and despite the fact that each pixel encloses many SPH particles with different distributions in the gas parameters, we model the emission of the gas as that coming out of a single PDR instead of considering two or more components. Using model emission we try to estimate $\chi^2$ of the line ratios of the pixel in a fit with two or more components. Since we consider transitions up to $J = 4 - 3$ for CO and 13CO, we have a total of 8 transitions, hence 8–4 = 4 degrees of freedom in our fits. The purpose of favouring one PDR component in the fitting procedure, is not to reduce the degrees of freedom, since for every added PDR component we loose five degrees of freedom, which could result in fits that are less significant.

The statistic we minimize in the fitting procedure is:

$$
\chi^2 = \sum_j \sum_i \left( \frac{r_{ij} - \sigma_{ij}}{\sigma_{ij}} \right)^2
$$

(2)

(Press et al. 2002), where $r_{ij}$ and $\sigma_{ij}$ are the observed values and assumed error bars of the line ratios of the pixel in the synthetic map. $r_m$ is the line ratio for the single PDR model whose parameter set we vary to minimize $\chi^2$. The index $i$ corresponds to the different combinations of line ratios. The line ratios we try to match are CO and 13CO ladders normalized to their $J = 1 - 0$ transition, in addition to the ratios of 13CO to the CO ladder. These add up to 10 different line ratios which are not independent, and the number of degrees of freedom remains 4 for the mechanically heated model (mPDR), and 5 for the PDR which does not consider mechanical heating.

In Figure 8, we show the fitted line ratios of the pixels labelled (A, B, C, D) in Figure 7. The first row, labelled A, corresponds to the central pixel in the map. For this pixel, 90% of the emission emanates from gas whose density is higher than 10 cm$^{-3}$, constituting 24% of the mass in that pixel. The normalized cumulative distribution functions for the gas density (blue curves) and CO(1-0) luminosity (red curves) are shown in the bottom panels of Figure 7. The blue dashed lines indicates the density where 10, 50 and 90% of the SPH particles have a density up to that value. The numbers in red, below these percentages, indicate the contribution of these particles to the total luminosity of that pixel. For instance, in pixel A 10% of the particles have a density less than $\sim$ 0.03 cm$^{-3}$ and these particles
Fig. 6: Line ratio maps for various transitions of CO and $^{13}$CO for the disk galaxy. The transition of the line in the numerator is specified at the top of each column, whereas that of the denominator is specified at the left of each row. For example, the panel in the third row of the second column corresponds to the line ratio map of $^{13}$CO (2-1)/CO(3-2); the species involved in the line ratio are specified at the top left corner of each panel. Ratios larger than unity are typical to the central regions $R < 2$ kpc. Line ratio maps between CO transitions are to the left zig-zagged line, whereas the remaining maps are for line ratios between $^{13}$CO and CO. Ratios involving $J \geq 3-2$ transitions trace the small scale structure of the molecular gas for $R > 2$ kpc.

contribute 0% to the luminosity of that pixel; at the other end, 90% of the particles have a density less than $\sim 100 \text{ cm}^{-3}$ and these particle contribute 48% to the luminosity of that pixel. In a similar fashion, the red dashed lines show the cumulative distribution function of the CO(1-0) luminosity of the SPH particles, but this time integrated from the other end of the $n$ axis. For example, 50% of the luminosity results from particles whose density is larger than 100 cm$^{-3}$. These particles constitute 9% of the gas mass in that pixel. The fits for PDR models that do not consider mechanical heating are shown in Figure 8. We see that these models fit ratios involving $J > 3-2$ transitions poorly compared to the mPDR fits, especially for the pixel A, B which are closer to the centre of the galaxy compared to pixels C and D. In the remaining rows (B,C,D) of Figure 8 we show fits for pixels of increasing distances from the centre of the galaxy. We see that as we move away further from the centre, the CO to $^{13}$CO ratios become flat in general, close to the elemental abundance ratio of $^{13}$C/C which is 1/40 (see the green curve in the bottom row). This is essentially because the lines of both species are optically thin at the outer edge of the galaxy, hence the emission is linearly proportional to the column density which is related to the mean abundance in the molecular zone. Another observation is that the distribution of the luminosity in a pixel becomes narrow at the edge of the galaxy. This is due to the low gas density and temperature in this region, where there are less SPH particles whose density is close to the critical density of the CO(1-0) line. We also see that $\Gamma_{\text{mech}}$ plays a minor role, where both fits for a PDR with and without $\Gamma_{\text{mech}}$ are equally significant. The parameters of the fits for the four representative pixels are listed in Table 2.

This fitting procedure can also be applied to the dwarf galaxy. The main difference in modelling the gas as a PDR in the disk and dwarf galaxy is that the mechanical heating in the dwarf is lower compared to the disk, thus it does not make a significant difference in the fits. In Figure A.2 the line ratio maps show small spatial variation, thus it is not surprising in having small standard deviations in the fit parameters in Table 2 of the dwarf galaxy compared to the disk galaxy.

5. Conclusion and discussion

In this paper, we have presented a method to model molecular species emission such as CO and $^{13}$CO for any simulation which
includes gas and provides a local mechanical heating rate and UV-flux. The method uses this local information to model the spatial dependence of the chemical structure of PDR regions assumed to be present in the substructure of the gas in the galaxy models. These are then used to derive brightness maps assuming the LVG approximation. The method for the determination of the emission maps together with the interstellar medium model of the hydrodynamic galaxy models constitute a complete, selfconsistent model for the molecular emission from a star forming galaxies’ ISM. We compute the emission of CO and $^{13}$CO in rotational transitions up to $J = 4 − 3$ for a model disk like galaxy and a dwarf galaxy. From the emission maps, line ratios were computed to constrain the physical parameters of the molecular as PDRs.

We conclude the following:

1. Excitation temperature correlates positively with mechanical feedback in equilibrium galaxies. This in turn increases for gas which is closer to the centre of the galaxy. The analysis presented in this paper allows estimates of mechanical feedback in galaxies which have high excitation temperatures in the centre such as those observed by, e.g. [MüHle et al. 2007]; [Israel 2009].

2. Fitting line ratios of CO and $^{13}$CO using a single mechanically heated PDR component is sufficient to constrain the local $\Gamma_{\text{mech}}$ throughout the galaxy within an order of magnitude, given the limitations of our modelling of the emission. The density of the gas emitting in CO and $^{13}$CO is better constrained to within half dex. This approach is not suitable in constraining the gas parameters of the dwarf galaxy, although the statistical quality of the fits is on average better than that of the disk galaxy.

3. Our approach fails in constraining the local UV-flux. It is under-estimated by two orders of magnitude in mechanically heated PDR fits, and over estimated by more than that in PDRs which do not account for mechanical feedback. This discrepancy is due considering one PDR component, where $J < 3 – 2$ CO lines are optically thick and trace very shielded gas. This discrepancy can be also explained by looking at the right column of Figure A1 where the most of the emission results from SPH particles which constitute a small fraction and the rest of the gas is not captured by the PDR modelling.

The main features of our PDR modelling with mechanical feedback is the higher number of degrees of freedom it allows compared to LVG models and multi-component PDR modelling. We fit 10 line ratios while varying four parameters in the case where $\Gamma_{\text{mech}}$ was considered, and 3 parameters when $\Gamma_{\text{mech}}$ was not. We note that the actual number of independent measurements of line emission of of CO and $^{13}$CO up to $J = 4 − 3$ is 8. In LVG modelling the number of free parameters is at least 5, since in fitting the line ratios we need to vary $T$, $n(H_2)$, $N$(CO), $N$(CO) and the velocity gradient. On the other hand PDRs assume elemental abundances and reaction rates, moreover the uncertainties in the PDR modelling could be much larger and depend on the micro-physics used in the PDR modelling [VasYum in et al. 2004; Röllig et al. 2007]. Thus LVG models have more free parameters compared to single PDR models used in our method. On the other hand, considering two PDR components increases the number of free parameters to 9. Thus rendering the fitting problem overdetermined with more free parameters than independent measurements. Although LVG models are simple to run compared to PDR models, they do not provide information about the underlying physical phenomena exciting the line emission, which renders them useless for constraining $\Gamma_{\text{mech}}$. Although a two component PDR model produces better “Xi-by-eye” fits, these fits are statistically less significant than a single PDR model, but physically relevant. The main disadvantage of PDR modelling is the amount bookkeeping required to run these models and they are computationally 10 times more demanding than LVG modelling, which is why we resorted to using interpolation tables.

5.1. Improvements and prospects

Our models have two main limitations: 1) we make implicit assumptions on the small scale structure of the galactic ISM and 2) we assume chemical equilibrium. The first limitation can be improved by performing higher spatial resolution, which would result in gas that is better resolved and is denser than the current maximum of $10^4$ cm$^{-3}$ in the disk galaxy. A resolution of $10^6$ cm$^{-3}$ in the gas allows us to consider transitions up to $J = 15 − 14$ which are more sensitive to $\Gamma_{\text{mech}}$ compared to the $J = 1 − 0$. Galaxy scale simulations which reach densities higher than $10^4$ cm$^{-3}$ have been performed by Narayanan & Hopkins (2013) and required about $3 \times 10^7$ particles, and our method could be easily scaled to post-process such simulations.

Having more data to fit helps in finding better diagnostics of $\Gamma_{\text{mech}}$ and narrower constraints for it. Another advantage in having emission maps for these high $J$ transitions is the increased number of degrees of freedom in the fits, which renders the PDR models we fit statistically more significant. Moreover it would be natural to consider multi-components PDR models in these fits, a dense-component fitting the $J > 4 − 3$ transitions and low-density component fitting the lower ones. These components are not independent, low-$J$ emission is also produced by the high density PDR components. The high density component PDR would generally have a filling factor 10 to 100 times lower than the low density component, thus the high density model contributes mainly to the high-$J$ transitions, whereas the low density models contributes mainly to the low-$J$ emission and less to the high-$J$ emission.

In producing the synthetic line emission maps, we have used the LVG emission from SPH particles which assume PDR models as the governing sub-grid physics. An accurate treatment of the radiative transfer entails constructing the synthetic maps by solving the 3D radiative transfer of the line emission using tools such as LIME (Brinch & Hogerheijde 2010). This would eliminate any possible bias in the fits. Currently we construct the emission maps by considering the mean flux of the emission of SPH particles modelled as PDR within a pixel. This results in a distribution in the emission as a function of gas density as seen in Figure 7 and Figure A1. In fitting the line ratios, we recover the mean physical parameters of the molecular gas in that pixel associated with these emission. Using tools such as LIME, the micro-turbulence line width would be treated in a more realistic way by using the actual local velocity dispersions in the small scale turbulent structure of the gas, as opposed to adopting a fiducial 1 km s$^{-1}$ as we have done throughout the paper.

Not all H$_2$ gas is traced by CO, since the H$_2$/CO transition zone occurs around $A_V = 0.1$ mag whereas the C/CO transition occurs around $A_V = 1$ mag. In looking at Figure 7 and Figure A1 we see that most of the CO emission emanates from a fraction of the gas. The remaining “major” part of the gas can contain molecular H$_2$ which is not traced by CO and could be traced by other species such as C or C$^+$ that could have high enough abundances to have bright emission [Wolff et al. 2010].

Finally, we note that we have ignored any “filling factor” effects in constructing the synthetic maps and in the fitting pro-
procedure. This is not relevant to our method since in considering line ratios, filling factors cancel out in single PDR modelling of line ratios. However it is important and should be taken into account when considering multi-component PDR modelling and when fitting the absolute luminosities.

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Fig. 7: Distributions of gas density and $W(\text{CO}(1-0))$ as a function of distance from the centre of the disk galaxy. The normalized $W_{\text{CO}(1-0)}$ map, with the overlaid grid which has a resolution of 21 × 21 pixels is shown in the Top panel. The labels A, B, C, D correspond to the pixels at distances of 0, 2, 4, and 7 kpc from the centre of the galaxy. In the bottom panels we plot, in blue, the gas density distribution function, $f(n)$, of the SPH particles in these pixels. The fractional contribution of the SPH particles to the CO(1-0) luminosity of the pixel as a function of gas density, $f(L_{\text{CO}(1-0)})(n)$, is plotted in red. Both curves are scaled to their maximum value so that we can compare the ranges where they overlap. The cumulative distribution function is defined as $\text{CDF}(n) = \int_{n}^{10^{-3}} f(n) dn$. The blue dashed lines indicate the gas densities where the CDF = 10, 50, 90% respectively. Below these percentages, in red, are the fractional contribution of these SPH particles to the luminosity of the pixel. This contribution is defined as $\text{LCDF}(n) = \int_{n}^{10^{-3}} f(L_{\text{CO}(1-0)})(n) dn$. The red dashed lines represent the LCDF = $\int_{n}^{10^{-4}} f(L_{\text{CO}(1-0)})(n) dn$ along with the analogous CDF integrated from $n = 10^{4}$ cm$^{-3}$. The corresponding distribution plots as a function of $G_0$, $\Gamma_{\text{mech}}$ and $A_V$ are shown in Figure A.1 in the appendix.

Fig. 8: Constraining the parameters for a resolved galaxy. The black dots correspond to the line ratios of CO($J \geq 2 - 1$) with CO(1-0) for a pixel in the emission map. The red dots correspond to the line ratios of $^{13}$CO ($J \geq 2 - 1$) with $^{13}$CO (1-0) for the same pixel. The green dots correspond to the line ratios of the same transitions of $^{13}$CO and CO for a pixel. The dashed line are the line ratios of these transitions of the best fit PDR model. The PDR models in the left column labelled “with mechanical heating” consider a range of possible $\Gamma_{\text{mech}}$ in the heating budget while fitting these line ratios (the dots), while the plots labelled “without mechanical heating” do not take $\Gamma_{\text{mech}}$ into account. The parameters of the best fit PDR models for each pixel are listed in Table 2.
Table 2: A comparison between the parameters fit using line ratios for the disk and dwarf galaxy. The listed numbers are the averages of the fit parameters for pixels at a specific distance from the centre, these distances are listed on the left of the Table. For the dwarf galaxy we only show the fit parameters for the central 0.5 kpc. For each pixel, we present the fit parameter (first row) for a mechanically heated PDR (mPDR), a pure PDR which does not consider mechanical feedback into its heating budget (second row), and the actual mean and standard deviation for these quantities for the SPH particles within the pixel of the luminosity map. In the last column the statistic we minimize per degree of freedom, $\chi^2_{\text{red}}$ is listed to compare the quality of the fits of the mPDR and the pure PDR models.

<table>
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<tr>
<th></th>
<th>log$_{10}[n/\text{cm}^{-3}]$</th>
<th>log$_{10}(G/\text{G}_0)$</th>
<th>log$<em>{10}[\Gamma</em>{\text{mech}}/\text{erg cm}^{-3} \text{s}^{-1}]$</th>
<th>$A_V/\text{mag}$</th>
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<td></td>
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<td></td>
<td>Actual 1.63 ± 0.1</td>
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<tr>
<td>7 kpc</td>
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<tr>
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Fig. A.1: Distribution functions as a function of $G_0$, $\Gamma_{\text{mech}}$ and $A_V$ for the representative pixels labelled A, B, C and D of Figure 7. The blue curves represent the distributions as a function of $G_0$ (first column), $\Gamma_{\text{mech}}$ (second column) and $A_V$ (third column). The red curves represent the fractional contribution of these distributions to the luminosity of their corresponding pixels. Both curves are normalized to their peak so that we can visually compare the subset of these distributions which contribute to the luminosity.
Fig. A.2: Line ratio maps for various transitions of CO and $^{13}$CO for the dwarf galaxy. The line ratios are generally spatially uniform and show slight variation, unlike the disk galaxy. These maps are also patchy, especially for line ratios involving $J = 3 - 2$ and $J = 4 - 3$ transitions. This is due to the low number of SPH particles with densities close to $10^{4}$ cm$^{-3}$ which are a pre-requisites for these transitions. See caption of Figure 6 for more details on interpreting the maps.